

10.1

$$F_1 = 89.0 \text{ N}$$

$$x_1 = 0.0191 \text{ m}$$

Since  $F = kx \rightarrow k = F/x$

$$\therefore k = F_1/x_1 = \frac{89.0 \text{ N}}{0.0191 \text{ m}} = 4659.7 \text{ N/m.}$$

Now that the spring constant is known, we can again use  $F = kx$  (Hooke's law) to determine  $F_2$  when  $x_2 = 0.0508 \text{ m}$ :

$$F_2 = kx_2 = (4659.7 \text{ N/m})(0.0508 \text{ m}) = 236.7 \text{ N.}$$

Rounded to three significant figures,

$$F_2 = \boxed{237 \text{ N}}$$

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10.2

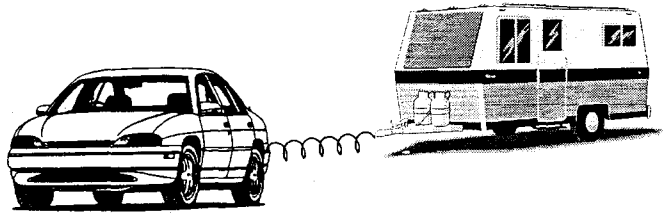
Hooke's law states for a spring,  $F = kx$ .

Since the bow string behaves as a spring with  $k = 480 \text{ N/m}$ , when a force  $F = 240 \text{ N}$  is applied

$$x = \frac{F}{k} = \frac{240 \text{ N}}{480 \text{ N/m}} = \boxed{0.50 \text{ m}}$$

10.5

In order to cause the 92 kg trailer to accelerate  $0.30 \text{ m/s}^2$ , the spring exerts a force given by



$$F = ma = (92 \text{ kg})(0.30 \text{ m/s}^2) = 27.6 \text{ N}$$

According to Hooke's law, the force exerted by a spring is related to the displacement by

$$F = -kx$$

Since  $k = 2300 \text{ N/m}$ ,

$$x = \frac{-F}{k} = \frac{-27.6 \text{ N}}{2300 \text{ N/m}} = \boxed{-0.012 \text{ m}}$$

The negative sign reflects that the force is in a direction opposite the displacement. So, if the car attempts to accelerate the trailer to the left, the spring is displaced (stretched) to the right by  $0.012 \text{ m}$ .

10.15

If we assume that the atoms vibrate with simple harmonic motion, then speed and acceleration are given by

$$v = -\omega A \sin(\omega t) \quad \#1 \quad \text{and} \quad a = -\omega^2 A \cos(\omega t) \quad \#2$$

Because sine and cosine functions have values that range from  $-1$  to  $+1$ , we see from eq #1 that speed is maximum when  $\sin(\omega t) = -1$ , and that acceleration in eq #2 is maximum when  $\cos(\omega t) = -1$ . Thus,

$$v_{\max} = \omega A \quad \#3 \quad \text{and} \quad a_{\max} = \omega^2 A \quad \#4$$

$$\text{Since } A = 1.1 \times 10^{-11} \text{ m}$$

$$\text{and } \omega = 2\pi f = 2\pi (2.0 \times 10^{12} \text{ cycle/s}) = 4\pi \times 10^{12} \text{ rad/s}$$

$$v_{\max} = (4\pi \times 10^{12} \text{ rad/s}) (1.1 \times 10^{-11} \text{ m}) = 138.23 \text{ m/s}$$

$$a_{\max} = (4\pi \times 10^{12} \text{ rad/s})^2 (1.1 \times 10^{-11} \text{ m}) = 1.7371 \times 10^{15} \text{ m/s}^2$$

Rounded to two significant figures,

$$v_{\max} = \boxed{140 \text{ m/s}} \quad \text{and} \quad a_{\max} = \boxed{1.7 \times 10^{15} \text{ m/s}^2}$$

10.24

$$x = 0.470 \text{ m}$$

$$k = 425 \text{ N/m}$$

a.  $P.E._{\text{elastic}} = \frac{1}{2} kx^2 = \frac{1}{2} (425 \text{ N/m})(0.470 \text{ m})^2 = 46.94125 \text{ J}$

Rounded to three significant figures,  $P.E._{\text{elastic}} = 46.9 \text{ J}$

b. If all of this potential energy is used to propel a 0.0300 kg arrow (that is, if this potential energy becomes the kinetic energy of the arrow), then

$$P.E._{\text{elastic}} = K.E._{\text{arrow}}$$

$$P.E._{\text{elastic}} = \frac{1}{2} m v^2 \rightarrow v = \pm \sqrt{\frac{2 P.E._{\text{elastic}}}{m}}$$

$$\therefore v = \pm \sqrt{\frac{2(46.9 \text{ J})}{0.0300 \text{ kg}}} = \pm 55.9 \text{ m/s}$$

10.31

$$m = 1.00 \times 10^{-2} \text{ kg}$$

$$k = 124 \text{ N/m}$$

$$v_1 = 8.00 \text{ m/s} \text{ when } x_1 = 0 \text{ m. (i.e. the spring is "unstretched")}$$

This problem is a study of the energies of simple harmonic motion. We know that kinetic energy is given by

$$\text{K.E.} = \frac{1}{2} m v^2 \quad \#1.$$

And we know that the potential energy of a spring is given by

$$\text{P.E.} = \frac{1}{2} k x^2 \quad \#2.$$

So by conservation of energy  $\text{K.E.}_1 + \text{P.E.}_1 = \text{K.E.}_2 + \text{P.E.}_2$  or

$$\frac{1}{2} m v_1^2 + \frac{1}{2} k x_1^2 = \frac{1}{2} m v_2^2 + \frac{1}{2} k x_2^2 \quad \#3.$$

Since  $x_2$  equals the amplitude  $A$  when  $v_2 = 0$ , eq #3 becomes

$$\frac{1}{2} m v_1^2 = \frac{1}{2} k A^2 \quad \#4$$

Solving for  $A$  in eq #4,

$$A = v_1 \sqrt{m/k} = 8.00 \text{ m/s} \sqrt{\frac{1.00 \times 10^{-2} \text{ kg}}{124 \text{ N/m}}} = 0.071842 \text{ m}$$

Rounded to three significant figures,

$$A = \boxed{0.0718 \text{ m}}$$

10.39

$$T = 2.0 \text{ s}$$

$$L = ?$$

$$\omega = \sqrt{g/L} \quad \text{and} \quad \omega = 2\pi f = \frac{2\pi}{T}$$

$$\therefore \frac{2\pi}{T} = \sqrt{g/L} \rightarrow L = g \left( \frac{T}{2\pi} \right)^2$$

$$L = 9.80 \text{ m/sec}^2 \left( \frac{2.0 \text{ s/cycle}}{2\pi \text{ rad/cycle}} \right)^2 = 0.99 \text{ m}$$

10.48

The response materials display to forces that either compress or stretch them is reflected by Young's modulus,  $Y$ , where

$$Y = \frac{F/A}{\Delta L/L_0} = \frac{\text{stress}}{\text{strain}} \quad \#1$$

From table 10.1, the Young's modulus for bone under compression is

$$Y = 9.4 \times 10^9 \text{ N/m}^2 \quad \#2$$

a. Since the stress =  $F/A$ , the maximum stress equals the greatest force  $F = 6.8 \times 10^4 \text{ N}$  divided by the smallest area  $A = 4.0 \times 10^{-4} \text{ m}^2$

$$\therefore \text{max. stress} = \frac{6.8 \times 10^4 \text{ N}}{4.0 \times 10^{-4} \text{ m}^2} = \boxed{1.7 \times 10^8 \text{ N/m}^2} \quad \#3$$

b. we can rearrange eq 1 to determine the strain.

$$\text{strain} = \frac{\text{stress}}{Y} = \frac{1.7 \times 10^8 \text{ N/m}^2}{9.4 \times 10^9 \text{ N/m}^2} = \boxed{0.018}$$

10.49

$$\Delta P = P_2 - P_1 = 0 - 1.01 \times 10^5 \text{ Pa} = -1.01 \times 10^5 \text{ Pa}$$

$$B_{\text{Al}} = 7.1 \times 10^{10} \text{ N/m}^2$$

$$\frac{\Delta V}{V_0} = ?$$

$$\text{Since } B \equiv \frac{-\Delta P}{\frac{\Delta V}{V_0}} \rightarrow \frac{\Delta V}{V_0} = \frac{-\Delta P}{B}$$

$$\therefore \frac{\Delta V}{V_0} = \frac{-(-1.01 \times 10^5 \text{ N/m}^2)}{7.1 \times 10^{10} \text{ N/m}^2} = \boxed{1.4 \times 10^{-6}}$$

10.69

The period of a simple pendulum is given by

$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$\therefore g = \frac{4\pi^2 l}{T^2}$$

We are given  $l = 1.2 \text{ m}$ . Since 100 cycles are completed in 280 s, the time required to complete one cycle (the period) is

$$T = \frac{280 \text{ s}}{100 \text{ cycles}} = 2.80 \text{ s/cycle}$$

$$\therefore g = \frac{4\pi^2 (1.2 \text{ m})}{(2.80 \text{ s/cycle})^2} = 6.0426 \text{ m/s}^2 *$$

Rounded to two significant figures,  $g = \boxed{6.0 \text{ m/s}^2}$

\* In case you are wondering, cycles (like radians) can be ignored.

10.71

The statue applies a force  $F = mg = (3500 \text{ kg})(9.80 \text{ m/s}^2)$  or



$$F = 34,300 \text{ N.}$$

$$A = 7.3 \times 10^{-2} \text{ m}^2$$

$$Y = 2.3 \times 10^{10} \text{ N/m}^2$$

$$L_0 = 1.8 \text{ m}$$

$$\Delta L = ?$$

Since  $Y = \frac{F/A}{\Delta L/L_0} \rightarrow \Delta L = \frac{F L_0}{Y A} = \frac{(34,300 \text{ N})(1.8 \text{ m})}{(2.3 \times 10^{10} \text{ N/m}^2)(7.3 \times 10^{-2} \text{ m}^2)} = \boxed{3.7 \times 10^{-5} \text{ m}}$

10.75

$$x_1 = 0.018 \text{ m}$$

$$m_1 = 2.8 \text{ kg}$$

$$m_2 = ? \quad \text{for } f_2 = 3.0 \text{ Hz.}$$

$$\text{Since } F_1 = kx_1 \rightarrow k = \frac{F_1}{x_1} = \frac{m_1 g}{x_1} = \frac{(2.8 \text{ kg})(9.80 \text{ m/s}^2)}{0.018 \text{ m}} = 1,524.44 \dots \text{ N/m}$$

Now that we know  $k$  for the spring we can use

$$\omega = \sqrt{\frac{k}{m}} \quad \# 1$$

to determine  $m$ .

From eq #1 and with  $\omega = 2\pi f$  we write

$$2\pi f = \sqrt{\frac{k}{m}} \rightarrow (2\pi f)^2 = \frac{k}{m}$$

$$\therefore m_2 = \frac{k}{(2\pi f_2)^2} = \frac{1,524.44 \dots \text{ N/m}}{[2\pi (3.0 \text{ cycles/s})]^2} = \boxed{4.3 \text{ kg}}$$