

13.1

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$$\left. \begin{aligned} T_2 &= 502^\circ\text{C} \\ T_1 &= 26^\circ\text{C} \end{aligned} \right\} \Delta T = 476^\circ\text{C}$$

$$L = 1.2\text{ m}$$

$$r = 5.0 \times 10^{-3}\text{ m} \rightarrow A = \pi r^2 = \pi (5.0 \times 10^{-3}\text{ m})^2 = 7.854 \times 10^{-5}\text{ m}^2$$

$$\Delta Q = ?$$

$$t = 5.0\text{ s}$$

$$k_{\text{iron}} = 79 \frac{\text{J}}{\text{s m}^\circ\text{C}}$$

$$\therefore \Delta Q = \frac{k A \Delta T t}{L} = \frac{(79 \frac{\text{J}}{\text{s m}^\circ\text{C}})(7.854 \times 10^{-5}\text{ m}^2)(476^\circ\text{C})(5.0\text{ s})}{1.2\text{ m}} = 12\text{ J}$$

13.4

The heat ΔQ that is transferred by conduction is expressed by the equation

$$\Delta Q = \frac{k A \Delta T t}{L}$$

We can compare the heat lost through the wool jacket to that lost through the down in the form of the ratio

$$\frac{\Delta Q_w}{\Delta Q_d} = \frac{k_w A_w \Delta T_w t_w / L_w}{k_d A_d \Delta T_d t_d / L_d}$$

Because the areas, temperature differences and time intervals are the same (i.e. $A_w = A_d$, $\Delta T_w = \Delta T_d$ and $t_w = t_d$) this ratio reduces to

$$\frac{\Delta Q_w}{\Delta Q_d} = \frac{k_w / L_w}{k_d / L_d} = \left(\frac{k_w}{k_d} \right) \left(\frac{L_d}{L_w} \right) = \frac{(0.040 \text{ J/s m } ^\circ\text{C}) (15 \text{ mm})}{(0.025 \text{ J/s m } ^\circ\text{C}) (5.0 \text{ mm})}$$

$$\frac{\Delta Q_w}{\Delta Q_d} = \boxed{4.8}$$

13.19

$$T = 3000^\circ\text{C} = 3273\text{ K}$$

$$P = 60\text{ W}$$

$$e = 0.36$$

$$A = ?$$

Since $\Delta Q = e\sigma T^4 A t$ and power $P = \frac{\text{Energy}}{\text{time}}$

$$A = \frac{\Delta Q}{e\sigma T^4 t} = \frac{(\Delta Q/t)}{e\sigma T^4} = \frac{P}{e\sigma T^4}$$

$$\therefore A = \frac{60\text{ W}}{(0.36)(5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4})(3273\text{ K})^4} = 2.6 \times 10^{-5} \text{ m}^2$$

13.20

By definition, intensity equals power divided by area, or

$$I = \frac{P}{A}$$

$$\text{So, } P = IA \quad \#1$$

Since the intensity of thermal radiation is

$$I = e \sigma T^4 \quad \#2,$$

eq 1 can be written as

$$P = e \sigma T^4 A \quad \#3$$

We can use eq 3 to determine T:

$$T = \left[\frac{P}{e \sigma A} \right]^{1/4} \quad \#4$$

The area A is the area of the surface of the sun, a sphere of radius

$$r = 6.96 \times 10^8 \text{ m.}$$

$$A = 4\pi r^2 = 4\pi (6.96 \times 10^8 \text{ m})^2 = 6.087 \times 10^{18} \text{ m}^2$$

$$\text{Since } P = 3.9 \times 10^{26} \text{ W}$$

and $e = 1$ (a black body)

eq 4 produces

$$T = \left[\frac{3.9 \times 10^{26} \text{ W}}{(1)(5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4})(6.087 \times 10^{18} \text{ m}^2)} \right]^{1/4} = \boxed{5800 \text{ K}}$$

13.27

$$A = 1.6 \text{ m}^2$$

$$L = 2.0 \times 10^{-3} \text{ m}$$

$$T_1 = 11^\circ\text{C}$$

$$T_2 = 36^\circ\text{C}$$

$$t = 1.0 \text{ s.}$$

$$k_{\text{wool}} = 0.040 \frac{\text{J}}{\text{m}^\circ\text{C}^\circ\text{s}}$$

$$\Delta Q = ?$$

$$\Delta Q = \frac{k A \Delta T t}{L} = \frac{(0.040 \frac{\text{J}}{\text{m}^\circ\text{C}^\circ\text{s}})(1.6 \text{ m}^2)(25^\circ\text{C})(1.0 \text{ s})}{2.0 \times 10^{-3} \text{ m}} = 800 \text{ J}$$

Thus, the heat lost per second, $\frac{\Delta Q}{t} = \frac{800 \text{ J}}{1.0 \text{ s.}} = \boxed{800 \frac{\text{J}}{\text{s}}}$

(3.3)

$$I = 560 \text{ W/m}^2$$

$$\text{Since } I = e\sigma T^4$$

$$T^4 = \frac{I}{e\sigma} \quad \text{or} \quad T = \left(\frac{I}{e\sigma}\right)^{1/4}$$

$$T = \left[\frac{560 \text{ W/m}^2}{(1)(5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4})} \right]^{1/4} = (9.8765 \times 10^9 \text{ K}^4)^{1/4} = 3.1525 \times 10^2 \text{ K}$$

Rounded to two significant figures, $T = \boxed{320 \text{ K}}$