

16.2

Ten cycles of waves are completed in 120 s. Because frequency is the number of cycles that occur divided by the time required for their completion,

$$f = \frac{10 \text{ cycles}}{120 \text{ s}} = \frac{1}{12} \text{ cycle/s} = \frac{1}{12} \text{ Hz} = \boxed{.083 \text{ Hz}}$$

NOTICE

This material may be
protected by copyright
law (Title 17 U.S. Code)

16.3

$$f = 3.0 \text{ Hz.}$$

$$t = 1.7 \text{ s.}$$

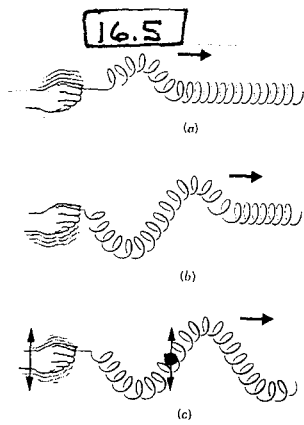
$$s = 2.5 \text{ m.}$$

$$\lambda = ?$$

$$\text{Since } s = v_{\text{ave}} t \rightarrow v_{\text{ave}} = \frac{s}{t} = \frac{2.5 \text{ m}}{1.7 \text{ s}} = 1.471 \text{ m/s.}$$

$$\text{Since } v = \lambda f \rightarrow \lambda = \frac{v}{f} = \frac{1.471 \text{ m/s.}}{3.0 \text{ cycles/s.}} = 0.4902 \text{ m/cycle.}$$

Rounded to two significant figures, $\lambda = \boxed{0.49 \text{ m}}$



Since "the hand moves the end of the slinky up and down through two complete cycles in one second," the frequency is

$$f = 2 \text{ cycles/s} \quad (\text{or } 2 \text{ Hz})$$

And since $v = 0.50 \text{ m/s}$,

$$\lambda = \frac{v}{f} = \frac{0.50 \text{ m/s}}{2 \text{ cycles/s}} = \boxed{0.25 \text{ m/cycle}}$$

16.13

$$F = 944 \text{ N.}$$

$$T = 3.82 \times 10^{-3} \text{ s/cycle}$$

$$\lambda = 1.26 \text{ m/cycle}$$

$$m/l = ? \text{ (the "linear density")}$$

Linear density and force are terms found in the equation for the speed of propagation of a transverse wave,

$$v = \sqrt{\frac{F}{m/l}} \quad \#1$$

Squaring both sides of eq #1 and solving for the linear density,

$$m/l = \frac{F}{v^2} \quad \#2$$

According to eq #2, we will need v , the speed of propagation. We can find v using

$$v = f\lambda \quad \text{and} \quad f = \frac{1}{T}$$

$$v = \frac{\lambda}{T} = \frac{1.26 \text{ m/cycle}}{3.82 \times 10^{-3} \text{ s/cycle}} = 329.8429319 \text{ m/s.}$$

Substituting this value into eq #2

$$m/l = \frac{944 \text{ N}}{(329.8429319 \text{ m/s})^2} = 0.0086767609 \text{ kg/m.}$$

Rounded to three significant figures,

$$m/l = \boxed{0.00868 \text{ kg/m}}$$

16.32

$$Y_{\text{steel}} = 2.0 \times 10^{11} \text{ N/m}^2$$

$$\rho_{\text{steel}} = 7860 \text{ kg/m}^3$$

$$\therefore v_{\text{steel}} = \sqrt{\frac{Y_{\text{steel}}}{\rho_{\text{steel}}}} = \sqrt{\frac{2.0 \times 10^{11} \text{ N/m}^2}{7860 \text{ kg/m}^3}} = 5044.33 \text{ m/s.}$$

From table #1 in this chapter, the speed of sound in air at 20°C is

$$v_{\text{air}} = 343 \text{ m/s.}$$

Therefore the speed of sound in steel compared its speed in air is given by the ratio

$$\frac{v_{\text{steel}}}{v_{\text{air}}} = \frac{5044.33 \text{ m/s}}{343 \text{ m/s}} = 14.7065$$

Rounded to two significant figures, sound travels 15 times faster in steel than it does in air.

16.48

$$A = 2.1 \times 10^{-3} \text{ m}^2$$

$$I = 3.2 \times 10^{-6} \text{ W/m}^2$$

$$P = ?$$

$$\text{Since } I = \frac{P}{A} \rightarrow P = IA = (3.2 \times 10^{-6} \text{ W/m}^2)(2.1 \times 10^{-3} \text{ m}^2) = 6.7 \times 10^{-9} \text{ W.}$$

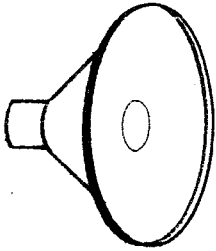
16.53

$$r = 0.0950 \text{ m.}$$

$$P_E = 25.0 \text{ W.} \quad (\text{electric power})$$

$$I_s = 17.5 \text{ W/m}^2 \quad (\text{actual sound intensity produced by speaker})$$

% converted to sound = ?



To determine the percentage of the electric power P_E converted into acoustic (or sound) power P_s , we must first calculate P_s :

$$\text{Since } I = \frac{P}{A} \rightarrow P = IA; \text{ and with } A = \pi r^2$$

$$P_s = I_s \pi r^2 = (17.5 \text{ W/m}^2) \pi (0.0950 \text{ m})^2 = 0.4961752 \text{ W.}$$

Now the ratio $\frac{P_s}{P_E}$ is the fraction of the electric power that is converted to sound; and when multiplied by 100, it is the percentage:

$$\left(\frac{P_s}{P_E}\right) 100 = \left(\frac{0.4961752 \text{ W}}{25.0 \text{ W}}\right) 100 = \boxed{1.98 \%}$$

16.72

The Doppler Effect equation for a source moving toward the observer and the observer moving toward the source is

$$f_o = f_s \left(\frac{v + v_o}{v - v_s} \right)$$

$$\therefore f_o = 3400 \text{ Hz} \left(\frac{330 \text{ m/s} + 39 \text{ m/s}}{330 \text{ m/s} - 18 \text{ m/s}} \right) = 4021.15 \text{ Hz.}$$

Rounded to two significant figures, $f_o = \boxed{4000 \text{ Hz.}}$

16.73

The Doppler effect formula is $f_o = f_s \left(\frac{v + v_o}{v + v_s} \right)$ # 1.

Assuming you (the observer) are stationary, $v_o = 0$. And we are told that $f_o = 0.86 f_s$. Substituting this information into eq # 1,

$$0.86 f_s = f_s \left(\frac{v}{v + v_s} \right) \rightarrow 0.86 = \frac{v}{v + v_s} \quad \# 2.$$

Eq # 2 can be rearranged to solve for v_s :

$$v_s = \frac{v}{0.86} - v = v \left[\frac{1}{0.86} - 1 \right]$$

with $v = 343 \text{ m/s}$,

$$v_s = 343 \text{ m/s} \left[\frac{1}{0.86} - 1 \right] = 55.8372 \text{ m/s}.$$

Rounded to two significant figures, $v_s = \boxed{56 \text{ m/s}}$.

16.85

$$\mu/L = 7.8 \times 10^{-4} \text{ kg/m}$$

$$f = 440 \text{ Hz.}$$

$$\lambda = 65 \text{ cm.} = 0.65 \text{ m} = 0.65 \text{ m/cycle}$$

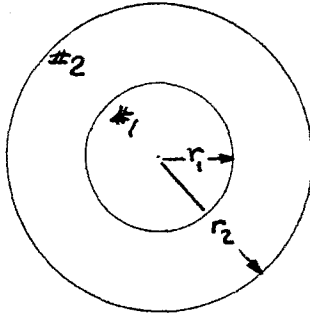
$$F = ?$$

$$\text{Since } v = \left(\frac{F}{\mu/L}\right)^{1/2} \rightarrow F = v^2(\mu/L) \quad \#1$$

$$\text{And, since } v = \lambda f = (0.65 \text{ m/cycle})(440 \text{ cycles/s}) = 286 \text{ m/s,} \quad \text{eq \#1 yields}$$

$$F = (286 \text{ m/s})^2 (7.8 \times 10^{-4} \text{ kg/m}) = \boxed{64 \text{ N}}$$

16.93



Intensity I varies with power P and area A according to the equation

$$I = P/A \quad \#1.$$

Assuming the acoustic power doesn't change (i.e. $P_2 = P_1$) as the travels from region #1 to region #2 and the sound is uniformly distributed over a spherical area (i.e. $A = 4\pi r^2$)

$$I_1 = P_1/A_1 = \frac{P_1}{4\pi r_1^2} \quad \#2 \quad \text{and} \quad I_2 = P_2/A_2 = \frac{P_2}{4\pi r_2^2} \quad \#3$$

Intensity level β is related to intensity by the equation

$$\beta = 10 \log(I/I_0) \quad \#4$$

$$\therefore \beta_1 = 10 \log(I_1/I_0) \quad \#5 \quad \text{and} \quad \beta_2 = 10 \log(I_2/I_0) \quad \#6$$

and the change in intensity level $\beta_2 - \beta_1$ is

$$\beta_2 - \beta_1 = 10 \log(I_2/I_0) - 10 \log(I_1/I_0) = 10 \log\left(\frac{I_2/I_0}{I_1/I_0}\right)^* = 10 \log\left(\frac{I_2}{I_1}\right) \quad \#7$$

Substituting eqs #2 and #3 into eq #7,

$$\beta_2 - \beta_1 = 10 \log\left(\frac{P_2/4\pi r_2^2}{P_1/4\pi r_1^2}\right) = 10 \log\left(\frac{r_1^2}{r_2^2}\right) = 10 \log\left(\frac{r_1}{r_2}\right)^2$$

$$\text{with } r_2 = 2r_1, \quad \beta_2 - \beta_1 = 10 \log\left(\frac{1}{2}\right)^2 = 10 \log\left(\frac{1}{4}\right) = \boxed{-6.0206 \text{ dB}}$$

* Notice: I used the logarithmic property

$$\log A - \log B = \log(A/B)$$

16.94

Intensity is given by the formula $I = \frac{P}{A}$

In this case, the power (which is energy divided by time) is

$$P = \frac{2.0 \times 10^5 \text{ J}}{1 \text{ s.}} = 2.0 \times 10^5 \text{ W}$$

Since the sound travels uniformly in all directions, we can assume that the sound spreads over a spherical surface of radius 85 m. Using the formula for the area of a sphere,

$$A = 4\pi r^2 = 4\pi (85 \text{ m})^2 = 90,792 \text{ m}^2$$

$$\text{Therefore } I = \frac{2.0 \times 10^5 \text{ W}}{90,792 \text{ m}^2} = 2.2028 \text{ W/m}^2$$

Now, to determine the corresponding intensity level,

$$\beta = 10 \log\left(\frac{I}{I_0}\right) = 10 \log\left(\frac{2.2028 \text{ W/m}^2}{1 \times 10^{-12} \text{ W/m}^2}\right) = 10 \log(2.2028 \times 10^{12}) = 123.42982 \text{ dB}$$

Rounding our answer to two significant digits,

$$\beta = \boxed{120 \text{ dB}}$$